



"QUADRATIC JAHN-TELLER COUPLING IN OCTAHEDRAL SYSTEMS"

by

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Prepared for Publication in Molecular Physics

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March 1978

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REPORT DOCUMENTATION PAGE	READ INSTRUCTIONS
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(14)TR-28	
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Quadratic Jahn-Teller Coupling in Octahedral	Technical Report.
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7. AUTHOR(a)	8. CONTRACT OR GRANT NUMBER(*)
E. R./Bernstein J. D./Webb	NAME 14-75-C-1179
Department of Chemistry	10. PROGRAM ELEMENT, PROJECT, T.
Colorado State University	NR 056-607
Fort Collins, Colorado 80523	
11. CONTROLLING OFFICE NAME AND ADDRESS	PEPORT DATE
Office of Naval Research	Mar. 78
Arlington, VA 22217	19
14. MONITORING AGENCY NAME & ADDRESS(II different from Controlling Office	Unclassified
	Unclassified
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Span the  $\mathbf{V}_{2}(e_{g})$  mode of MF<sub>6</sub> systems. Calculational details are discussed. It is concluded that, in agreement with previously reported spectroscopic data for ReF<sub>6</sub> and IrF<sub>6</sub>, quadratic terms in the vibronic interaction are essential (both qualitatively and quantitatively) to the complete understanding of intrastate vibronic coupling in transition metal hexafluorides.

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#### INTRODUCTION

Recent experimental studies of transition metal hexafluorides  $^{1-3}$  have indicated that the spectroscopically observed dynamic Jahn-Teller (JT) effects are not adequately explained by the usual linear JT theory  $^4$ ; quadratic terms, at least, are required in the vibronic Hamiltonian. In order to treat hexafluoride data quantitatively, it would be desirable to solve the problem of two JT-active vibrations ( $v_2$  ( $e_g$ ) and  $v_5$  ( $t_{2g}$ )) vibronically coupled to a  $r_{8g}$  electronic state for a Hamiltonian complete up to quadratic terms [ $r_{8g} \times (e_g + t_{2g})$ ] QUAD. Unfortunately, however, the requisite numerical methods are not feasible given currently available computers. In fact, even the [ $r_{8g} \times t_{2g}$ ] QUAD problem alone presents an arduous task. The [ $r_{8g} \times e_g$ ] QUAD coupling problem is, however, readily soluble. Its solution is presented here and is found to generate a qualitative insight into the nature of the quadratic portion of the JT interaction.

Previous work on  $[\Gamma_{8g} \times e_g]_{QUAD}$  (or the very closely related problem:  $[E_g \times e_g]_{QUAD})^4$  has focused on the weak coupling limit<sup>5</sup> or on the case for which linear coupling is large.<sup>6</sup> In the present work matrix elements are given which allow full secular matrices for  $[\Gamma_{8g} \times e_g]_{QUAD}$  to be set up and diagonalized numerically. Given a sufficiently large enough truncated secular matrix, accurate eigenvalues and eigenvectors can be obtained for any values of the linear and quadratic parameters. These secular matrices are also applicable to the  $[E_q \times e_q]_{QUAD}$  situation.

### II. THEORY

The first step toward obtaining the necessary matrix elements for  $[r_{8g} \times e_g]_{QUAD}$  is to find the vibronic Hamiltonian. Englman<sup>4</sup> has discussed in detail the group theoretical techniques which allow a parametric Hamiltonian to be obtained; it is given here with only minor modifications:

$$\widehat{\mathcal{H}} = \widehat{\mathcal{H}}^{(o)} + \widehat{\mathcal{H}}^{(i)} + \widehat{\mathcal{H}}^{(2)}_{(a_{iq})} + \widehat{\mathcal{H}}^{(2)}_{(e_q)} + \dots$$
 (1)

in which

$$\widehat{\mathcal{H}}^{(c)} = \left\{ \underline{I} \left( \hat{\rho}_{\theta}^{2} + \hat{\rho}_{\epsilon}^{2} \right) + \underline{k_{\epsilon}} \left( g_{\theta}^{2} + g_{\epsilon}^{2} \right) \right\} \underline{I} , \qquad (2)$$

$$\widehat{\mathcal{H}}^{(i)} = \mathcal{L}_{\epsilon} \left( g_{\theta} \underline{P}_{1} + g_{\epsilon} \underline{P}_{2} \right), \tag{3}$$

$$\widehat{\mathcal{H}}_{(a,q)}^{(2)} = \frac{C_a}{2} \left( g_{\theta}^2 + g_{\epsilon}^2 \right) \underline{I} , \qquad (4)$$

and

$$\widehat{\mathcal{F}_{6}}^{(2)}(e_{g}) = C_{\epsilon} \left\{ \left( g_{\theta}^{2} - g_{\epsilon}^{2} \right) \underline{P}_{\epsilon} - 2 g_{\theta} g_{\epsilon} \underline{P}_{2} \right\}. \tag{5}$$

 $(g_{\theta},g_{\epsilon})$  are the mass-weighted normal coordinates of the  $e_g$  vibration,  $(\hat{P}_{\theta},\hat{P}_{\epsilon})$  are the conjugate mass-weighted momenta,  $k_{\epsilon}$  is the vibrational force constant,  $\underline{I}$  is the 4 x 4 identity matrix,  $(\mathfrak{l}_{\epsilon},\,C_a,\,C_{\epsilon})$  are the linear and quadratic coupling parameters, and  $(\underline{P}_{\epsilon},\,\underline{P}_{\epsilon},\,\underline{P}_{\epsilon})$  are Dirac matrices.  $\underline{A}$  In the following discussion we will also make use of  $\underline{\sigma}_{1},\,\underline{\sigma}_{2},\,\underline{\sigma}_{3}$ , which are additional Dirac matrices as given in reference 4.

Choice of vibronic basis set is important since many matrix elements need to be calculated. In any case, the basis will involve two-dimensional harmonic

oscillator functions,  $\{X(n_2,\ell_2)\}$  and vectors which represent the four electronic components  $\{\vec{V}(\rho_3,\sigma_3)\}$ . The  $\{\vec{V}(\rho_3,\sigma_3)\}$  are eigenvectors of both  $\underline{\rho_3}$  and  $\underline{\sigma_3}$  with eigenvalues  $\rho_3=\pm 1$  and  $\sigma_3=\pm 1$ . The question of how to combine these factors into a vibronic basis set that is most convenient is now addressed.

One approach, which will only be outlined, involves utilizing molecular point group theory. The vibrational factors, however, do not transform as standard irreducible representations of  $0_h^\star$  but appropriate linear combinations of these functions can be generated which do so transform. The symmetrized vibrational factors and the electronic factors, which transform as  $\Gamma_{8g}$ , can be combined using Clebsh-Gordon coefficients to give vibronic functions which transform as  $\Gamma_{6g}$ ,  $\Gamma_{7g}$ , or  $\Gamma_{8g}$ . Separate secular matrices can then be formed in the usual fashion. This method will not be used, however, because the calculation of matrix elements within this basis set is more cumbersome than need be.

An alternate approach is to use the same vibronic basis that is used in the linear problem. These are written as follows:

$$\vec{b}$$
 (n<sub>2</sub>,  $\ell_2$ ;  $\rho_3$ ,  $\sigma_3$ ; J<sub>2</sub>) = X(n<sub>2</sub>, $\ell_2$ )  $\vec{V}$  ( $\rho_3$ ,  $\sigma_3$ )

in which

$$J_2 = \ell_2 + \frac{\rho_3}{2} = \pm 1/2, \pm 3/2,...$$
  
 $n_2 = 0, 1, 2,...; \ell_2 = -n_2, -n_2 + 2, ..., n_2$   
 $\rho_3 = \pm 1, \sigma_3 = \pm 1.$ 

In linear coupling,  $J_2$  is a good quantum number and separate secular matrices are generated for each value of  $J_2$ . Upon introduction of quadratic terms ( $\mathcal{H}^{(2)}(e_g)$  in particular),  $J_2$  ceases to be a good quantum number. One can determine, by examining a general matrix element, that  $\{2J_2 \mod 3\}$  remains a good quantum number. Therefore, the following three sets of basis vectors, labeled by  $J_2$ , are coupled by the quadratic terms:

$$\{\pm 3/2, \pm 9/2, \pm 15/2...\}$$
 (0 mod 3),  
 $\{\ldots, -5/2, \pm 1/2, \pm 7/2, \ldots\}$  (1 mod 3),  
 $\{\ldots, -7/2, -1/2, \pm 5/2, \ldots\}$  (2 mod 3).

It is of interest to correlate the {2  $J_2 \mod 3$ } quantum number with irreducible representations of  $0_h^*$ . It can be shown that {0 mod 3} correlates with  $\Gamma_{6g}$  and  $\Gamma_{7g}$  while both {1 mod 3} and {2 mod 3} correlate with  $\Gamma_{8g}$ . Thus, one disadvantage of this basis set is that the {0 mod 3} block is not factored as much as possible (separate  $\Gamma_{6g}$  and  $\Gamma_{7g}$  sets); nonetheless, with modern computers and diagonalization routines, this is not a serious drawback.

The main task remaining is to find integrals of powers of vibrational coordinates over harmonic oscillator functions; these are often referred to as the primitive matrix elements. General formulae exist which allow these matrix elements to be evaluated simply.

Primitive matrix elements relevant to the case at hand are:

$$\int X^*(n_2, \ell_2)q_+ X(n_2 + 1, \ell_2 + 1)d\tau = \left\{\frac{1}{2\alpha} (n_2 + \ell_2 + 2)\right\}^{1/2}, \tag{7}$$

$$\int X^*(n_2, \ell_2)q_{\frac{1}{2}}^2 X(n_2 + 2, \ell_2 + 2)d\tau = \frac{1}{2\alpha} \left\{ (n_2 + \ell_2 + 2)(n_2 + \ell_2 + 4) \right\}^{1/2}, \quad (8)$$

$$\int X^*(n_2, \ell_2)q_{\frac{1}{2}}^2 X(n_2, \ell_2 \pm 2) d\tau = \frac{1}{2\alpha} \left\{ 4(n_2 \mp \ell_2)(n_2 \pm \ell_2 + 2) \right\}^{1/2}, \qquad (9)$$

$$\int X^{*}(n_{2}, \ell_{2})q_{+}q_{-}X(n_{2} + 2, \ell_{2})d\tau = \frac{1}{2\alpha} \left\{ (n_{2} - \ell_{2} + 2)(n_{2} + \ell_{2} + 2) \right\}^{1/2}, \quad (10)$$

$$\int X^*(n_2, \ell_2)q_+q_-X(n_2, \ell_2)d\tau = \frac{1}{2\alpha} \{2n_2 + 2\}$$
, (11) in which

$$q_{+} = q_{\theta} + iq_{\epsilon}$$

$$\alpha = \frac{\omega_{\epsilon}}{\hbar} = \frac{k_{\epsilon}^{k_{2}}}{\hbar}.$$

The desired vibronic matrix elements are then readily found:

$$\int_{b}^{+} (n_{2}, \ell_{2}; \rho_{3}, \sigma_{3}; J_{2}) \frac{2}{\hbar \omega_{\epsilon}} (1)_{b}^{+} (n_{2} + 1, \ell_{2} + \rho_{3}; -\rho_{3}, \sigma_{3}; J_{2}) d\tau =$$

$$\{D_{2}(n_{2} + \rho_{3}\ell_{2} + 2)\}^{-1/2}, \qquad (12)$$

$$\int_{b}^{+} (n_{2}, \ell_{2}; \rho_{3}, \sigma_{3}; J_{2}) \frac{\partial e}{\partial t} (2) (a_{1g}) \dot{b}(n_{2}, \ell_{2}; \rho_{3}, \sigma_{3}; J_{2}) d\tau = \frac{Q_{2}[a_{1g}]}{2} \{n_{2} + 1\}, (13)$$

$$\int_{0}^{+} (n_{2}, \ell_{2}; \rho_{3}, \sigma_{3}; J_{2}) \frac{\mathcal{E}^{(2)}}{\hbar \omega_{\epsilon}} (a_{1g}) \dot{b} (n_{2} + 2, \ell_{2}; \rho_{3}, \sigma_{3}; J_{2}) d\tau =$$

$$\frac{Q_2[a_{1g}]}{4} \{ (n_2 + \ell_2 + 2)(n_2 - \ell_2 + 2) \}^{1/2},$$
 (14)

$$\int_{b}^{+} (n_{2}, \ell_{2}; \rho_{3}, \sigma_{3}; J_{2}) \underbrace{\widehat{\mathcal{H}}^{(2)}}_{h \omega_{\epsilon}} (e_{g})_{b}^{+} (n_{2}, \ell_{2}-2\rho_{3}; -\rho_{3}, \sigma_{3}; J_{2}-3\rho_{3}) d\tau =$$

$$Q_{2}[e_{q}]\{4(n_{2} + \rho_{3}\ell_{2})(n_{2} - \rho_{3}\ell_{2} + 2)\}^{1/2},$$
(15)

$$\int_{0}^{+} (n_{2}, \ell_{2}; \rho_{3}, \sigma_{3}; J_{2}) \frac{\hat{\mathcal{H}}^{(2)}}{\hbar \omega_{\epsilon}} (e_{g}) \dot{b} (n_{2} + 2, \ell_{2} - 2\rho_{3}; -\rho_{3}, \sigma_{3}; J_{2} - 3\rho_{3}) d\tau =$$

$$Q_{2}[e_{g}] \{(n_{2} - \rho_{3}\ell_{2} + 2)(n_{2} - \rho_{3}\ell_{2} + 4)\}^{1/2},$$
(16)

in which the dimensionless coupling parameters are defined as:  $D_2 = \frac{k_E^2}{2\hbar \omega_E^3}$ ,

$$Q_2[a_{1g}] = \frac{C_a}{k_c}$$
,  $Q_2[e_g] = \frac{C_c}{2k_c}$ .

Note that  $\sigma_3$  does not appear on the right hand side of any of these equations and thus two identical secular matrices are generated, one for each value  $(\pm 1)$  of the quantum number  $\sigma_3$ . It will prove to be interesting, for later considerations (see Section III), to use perturbation theory to find the splitting of the  $n_2 = 1$  level due to  $\mathcal{F}^{(2)}(e_g)$  in the unrealistic case of  $D_2 = 0$  (no linear coupling). The secular determinant which results from a first order degenerate perturbation theory treatment of the  $n_2 = 1$  level, employing equation 15, is

$$\begin{vmatrix} (2 - \lambda) & 4 & Q_2[e_g] \\ 4Q_2[e_g] & (2 - \lambda) \end{vmatrix} = 0$$
 (17)

with solutions

$$\lambda \approx 2 + 4 Q_2[e_g].$$

These quantities are measured in units of vibrational energy,  $\hbar\omega_{\epsilon}$ . It is possible to obtain a first order expression for  $\hat{\mathcal{L}}^{(2)}(a_{1g})$  also; however, this is not necessary since an exact expression easily obtains:

$$\lambda = (n_{\epsilon} + 1) \sqrt{1 + Q_2[a_{1g}]} = (n_{\epsilon} + 1)(1 + \frac{Q_2[a_{1g}]}{2} + \dots) . \quad (18)$$

### III. DISCUSSION

Examples of the secular matrix calculation of energy levels of  $[r_8 \times e_g]_{QUAD}$  are given in Figures 1 and 2. The secular matrix used in these calculations was truncated after  $n_2$  = 10; a basis of this size results in 44 x 44 matrices for both the {0 mod 3} and {1 mod 3} blocks (the {2 mod 3} block gives the same eigenvalues as {1 mod 3}). Under these circumstances it is required that  $D_2$  be less than 1 for an accurate description of the levels. The upper limit of  $Q_2[e_g]$  was not numerically determined, but is probably about 0.5. The behavior of the levels at these large values of  $D_2$  and  $Q_2[e_g]$  is quite complicated due to specific level repulsions.

 $D_2$  may be taken as positive since the relevant matrix elements are all off-diagonal (Eqn. 12). The situation with respect to  $Q_2$  [e $_g$ ] is more complicated even though it too has all off-diagonal matrix elements in the employed linear JT basis (Eqn. 15, 16).  $\widehat{\mathcal{H}}^{(2)}$  (e $_g$ ) will have diagonal matrix elements in a symmetry adapted basis set. The eigenvalues of  $\widehat{\mathcal{H}}^{(2)}$  (e $_g$ ) are independent of the sign of  $Q_2$  [e $_g$ ], however, the concomitant changes in the eigenvectors upon changing the sign of  $Q_2$  [e $_g$ ] may alter their symmetry transformation properties. For  $Q_2$  [e $_g$ ]  $\rightarrow$   $Q_2$  [e $_g$ ],  $\Gamma_6 \rightarrow \Gamma_7$  and  $\Gamma_7 \rightarrow \Gamma_6$ .

Several general observations can be made based on these calculations:

- i) For the case  $D_2$  = 0 (Figure 1), the perturbation expression Eq. 17 is found to be useful over a large range of  $Q_2[e_g]$  values ( $Q_2[e_g] < 0.1$ ) by direct comparison with results of the truncated secular equation calculation. This situation arises because  $\mathscr{Z}^{(2)}(e_g)$  couples  $n_2$  and  $n_2 \pm 2$  levels, but not  $n_2$  and  $n_2 \pm 1$ , as in the linear case.
- ii) In the regime  $(D_2 < 0.2, Q_2[e_g] \le 0.05)$ , for the  $n_2 = 1$  levels, effects of linear and quadratic terms are found to be approximately independent; that is, the  $(n_2 = 1, J_2 = 1/2)$  level is not shifted appreciably as  $Q_2[e_g]$  increases, center-

of-gravity of the  $(n_2 = 1, J_2 = 3/2)$  levels is preserved, and splitting of  $(n_2 = 1, J_2 = 3/2)$  is approximately the same as in the  $D_2 = 0$  case.

iii) Behavior of the  $n_2$  = 2 levels are, however, qualitatively different from those of  $n_2$  = 1 (see Figures 1 and 2); one difference is in the behavior of the  $(n_2$  = 2, J = 3/2) levels (Figure 1). For  $D_2$  = 0, these levels do not split under  $\mathcal{Z}^{(2)}(e_g)$ , whereas  $D_2 \neq 0$  allows admixture of  $n_2$  = 1,3,... levels, thus causing  $(n_2$  = 2,  $J_2$  = 3/2) to split. It should be noted that existing perturbative treatments of  $\mathcal{Z}$  are not able to generate this splitting,  $n_2$  although a more complete perturbation calculation would, of course, reproduce these results.

Based on the form of the perturbation energy expressions for the linear and quadratic JT terms, it can be seen that certain  $n_2$  levels are split by  $\mathcal{L}^{(2)}(e_g)$  in the first order of perturbation theory (e.g., Eq. 17) while the same  $n_2$  levels are split by  $\mathcal{L}^{(1)}$  only in the second order. It is thus possible for quadratic JT terms to be more effective at splitting vibronic levels than are linear JT terms. Examination of the perturbation expressions for the  $n_2 = 1$  levels verifies this idea:

$$\lambda \left( \underbrace{\hat{\mathcal{H}}}_{(1)}^{(1)} \right) = 2 \pm 2(D_2^{\frac{1}{2}})^2$$

$$\lambda \left( \underbrace{\hat{\mathcal{H}}}_{(2)}^{(2)}(e_g) \right) = 2 \pm 4Q_2[e_g]. \tag{19}$$

 $D_2^{\frac{1}{2}}$  is used for comparison with  $Q_2[e_g]$  since it is proportional to  $\ell_{\epsilon}$  just as  $Q_2[e_g]$  is proportional to  $C_{\epsilon}$ . Thus, for  $D_2^{\frac{1}{2}} = Q_2[e_g] = 0.1$ , Eqs. 19 show that the splitting induced by  $\hat{\mathcal{H}}^{(2)}(e_g)$  is an order of magnitude more than that induced by  $\hat{\mathcal{H}}^{(1)}$ . Similar results obtain for  $\hat{\mathcal{H}}^{(2)}(a_{1g})$  (see Eq. 18).

Available hexafluoride data  $^{1-3}$  show that the splitting induced by the linear terms is of the same order of magnitude as the quadratically-induced splittings and shifts. Although these data indicate the expansion of  $\mathcal{H}$  in powers of  $q_{\theta}$  and  $q_{\varepsilon}$  is not converging as rapidly as might be desired, the entire effect cannot be attributed to non-linearity of  $\mathcal{H}$ . Greater effectiveness of  $\mathcal{H}^{(2)}(e_g)$  and  $\mathcal{H}^{(2)}(a_{1g})$  in causing shifts and splittings is also an important consideration.

### IV. CONCLUSION

An accurate numerical method is given for treating vibronic coupling of  $\Gamma_{8g}$  (0\*) electronic state to an  $e_g$  vibration for a vibronic Hamiltonian with linear and quadratic terms. Examples of the calculation are given and general comments on the behavior of the levels under the influence of quadratic terms are made. It is also found that the quadratic coupling term is a more effective perturbation than the linear coupling term with respect to the observed spectroscopic splitting.

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Figure 1.

Quadratic Jahn-Teller calculation for coupling of a  $\Gamma_8$  electronic state with a  $\nu_2(e_g)$  vibration,  $(\Gamma_8 \times e_g)_{QUAD}$ . The fixed parameter values are  $D_2 = 0$  and  $\nu_2^\circ = 670~{\rm cm}^{-1}$ .  $D_2$  is the linear Jahn-Teller coupling parameter and  $\nu_2^\circ$  is the unperturbed  $\nu_2$  harmonic oscillator frequency.  $Q_2$   $[e_g]$  is the quadratic coupling parameter. Note the large range over which the splitting is linear in  $Q_2$   $[e_g]$ . In the method employed here,  $\Gamma_6$  and  $\Gamma_7$  levels both arise from the same secular matrix ( the {0 mod 3} block, see text). The symmetry labels of the eigenvectors are generated from their transformation properties. Changing the sign of  $Q_2$   $[e_g]$  will not alter the energies, but will interchange  $\Gamma_6$  and  $\Gamma_7$  symmetry labels.

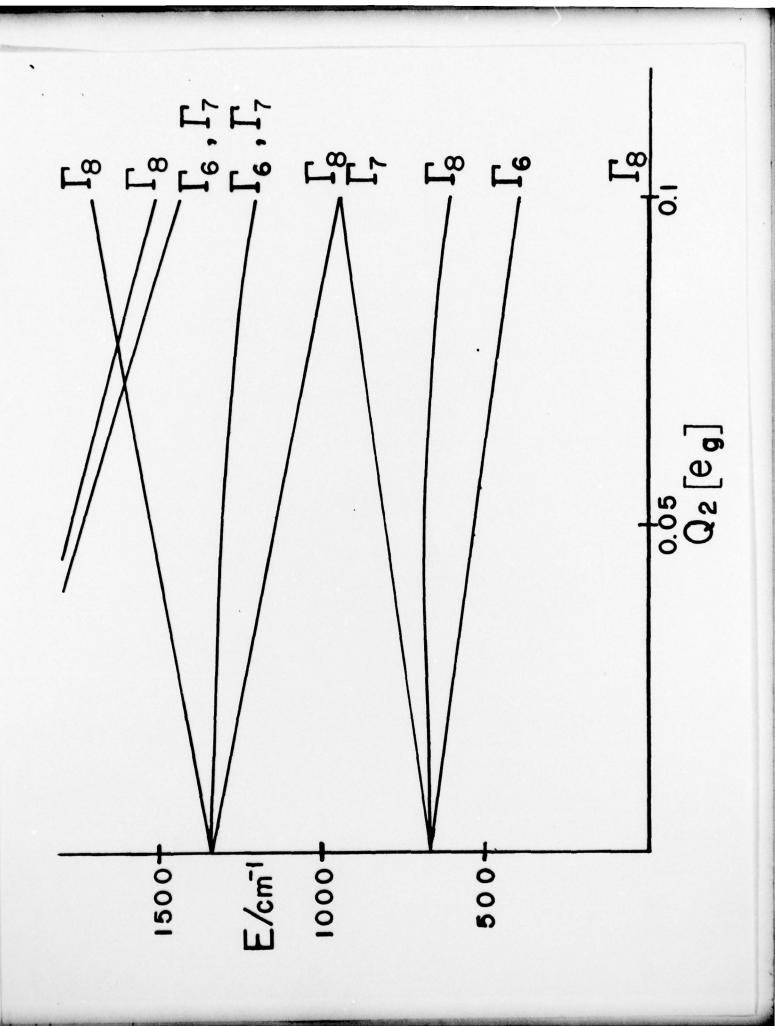
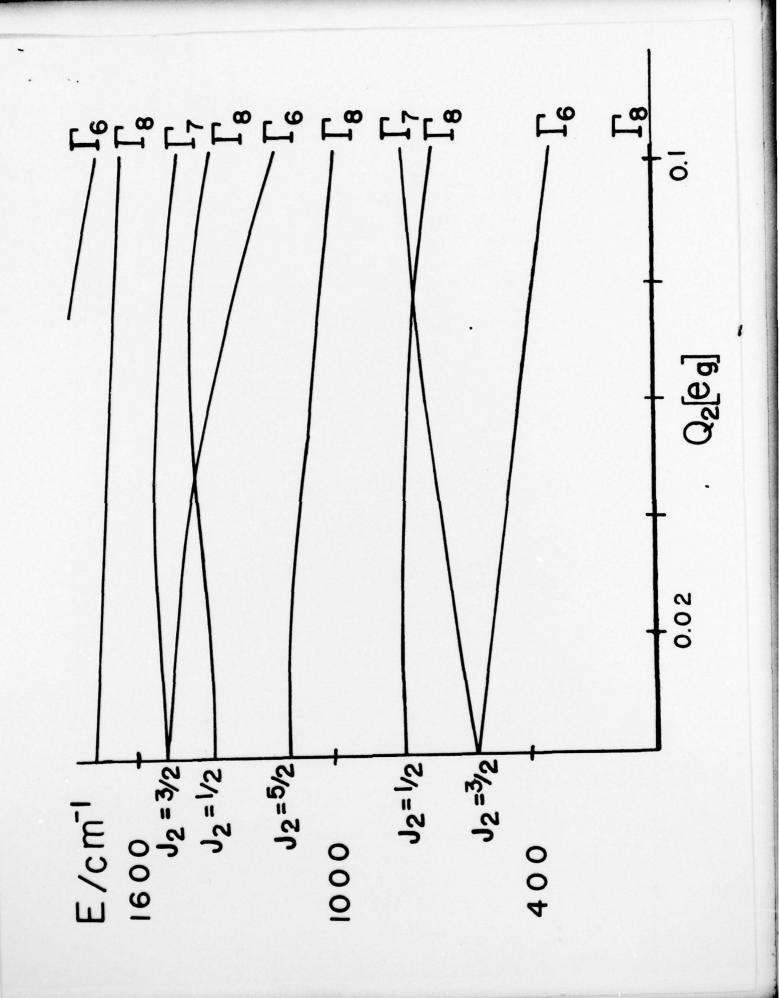


Figure 2.

Similar to Figure 1 but  $D_2$  has been set to 0.125. Note that the  $n_2$  = 1 for this value of  $D_2$  levels behave similarly to those for which  $D_2$  = 0 in that one pair of levels splits symmetrically and the other level remains largely uneffected as  $Q_2$  [e<sub>g</sub>] varies. This situation does not hold, however, for the  $n_2$  = 2 levels. The  $J_2$  quantum number, which is good at  $Q_2$ [e<sub>g</sub>] = 0, is indicated.



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